

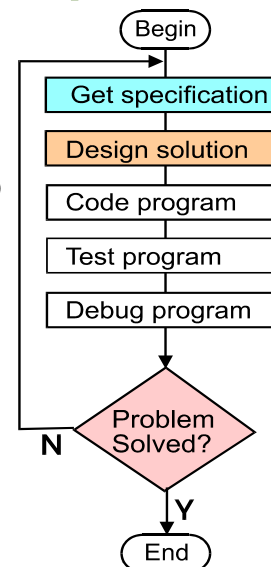
## Topic 2: Specification and design

1. Specification and UML
2. Object-oriented design
3. Modular decomposition
4. Algorithm-design tools
5. Functions and computation



## The system development process

- Development process is iterative
- **Specification**
  - Understanding the problem
  - input; output; their relationship
  - Unified Modeling Language
- **Design**
  - Language-independence
  - Module hierarchies, flowcharts, pseudocode
  - Coding, testing come later



## Four CS I skills objectives

- Vague specification → precise specification (analysis)
- Problem specification → flowchart (design)
- Flowchart → trace (design verification)
- Flowchart → program (coding)
- Program → trace (testing)

## 1. Specification and UML

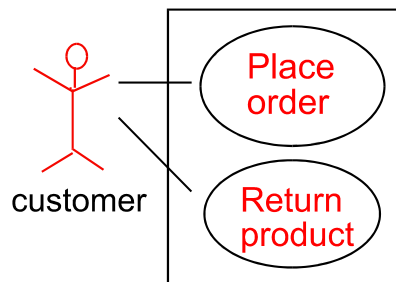
- **Unified Modeling Language:** a standard graphical notation for system specification and design
- Motivated by need to depict interactions between systems and their environments, initiated by external *actors*
- Diagrams include *use-case, activity, class, state, interaction*
- Supports an *object-oriented* methodology

## Software projects start with problem descriptions

- What service must the software provide?  
*Example: Process customer orders from catalog*
- What assumptions are made?  
*Example: Some customers may find Web access convenient*
- What risks are involved?  
*Example: Some users are inexperienced with Web access*

## Use cases and system specification

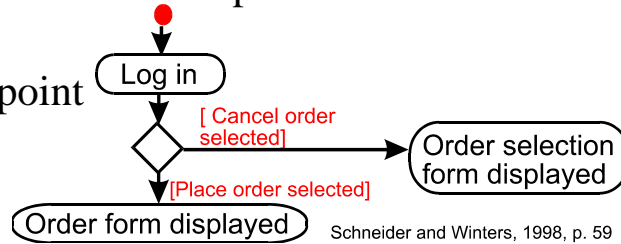
- Use case: A typical interaction between system and an *actor* in its environment
- Actor: A role, such as customer, manager, supplier, salesperson
- Actors initiate use cases
- Example of two uses cases (UML use-case diagram):



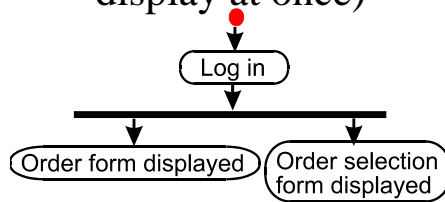
## UML activity diagrams

- Depict order in which steps occur

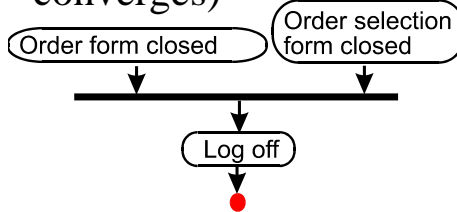
- *Examples:*  
A decision point (branching)



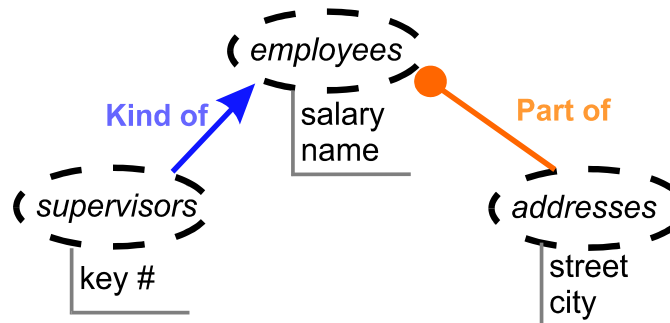
- A fork (2 forms display at once)



- A join (execution converges)



## 2. Object-oriented design



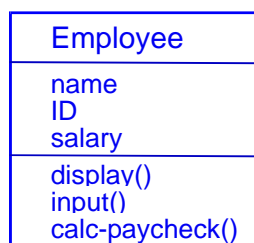
- Object-oriented design focuses on classes of objects and their attributes and behaviors

## The object-oriented paradigm

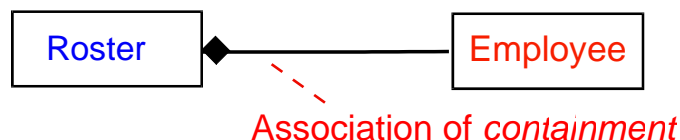
- *Object*: An instance of a class
- *Class*: A category defined by data *attributes* (properties) and *operations* (“methods”)
- In object-oriented programming, objects interact with each other via *messages*
- Objects may *contain* other objects
- Subclasses may *inherit* from other classes
- *Example*: Right-clicking an icon displays the properties and methods of the class of the object the icon represents

## UML class diagrams

- Rectangle with 3 horizontal compartments

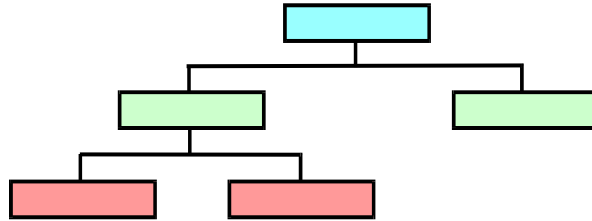


- Class association diagram



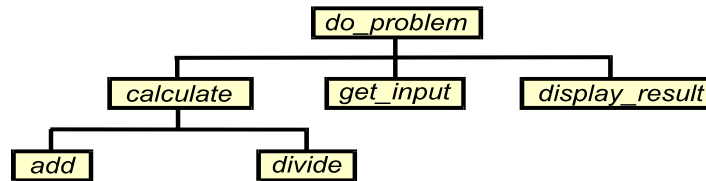
### 3. Modular decomposition

- One strategy: divide and conquer
- All programming languages support modularity
- An organization is modular



- Modular design may be *top-down*
- Subprograms implement modular designs

### Module hierarchy charts tell which subprogram uses which



- Module *do\_problem* uses modules *calculate*, *get\_input* and *display\_result*
- *calculate* uses *add* and *divide*
- Stepwise refinement may lead to further decomposition
- Module hierarchy contains names, not steps, in contrast to flowchart

## Guidelines for writing subprograms

- A module has a single purpose
- Its purpose is documented in a comment at the top
- Code longer than a page usually should be broken down
- Experienced programmers avoid side effects (e.g., output, modification of global variables)

## A divide-and-conquer strategy to solve problem of walking $n$ steps

**Walk (steps)**

If **steps** > 0

Take a step

Walk (**steps** – 1)

- This algorithm is *recursive* because it uses itself

## Binary phone-book search

Search key:  
"Simmons"

ABCDEF GHIJK LMNOP QR **S** TUVWXYZ

First try:  
"Simmons"  
is after M

Third try:  
"Simmons"  
is after P

Fourth try:  
"Simmons"  
is after R

Second try:  
"Simmons"  
is before T

- Each step eliminates half the unsearched data, cuts remaining work in half

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


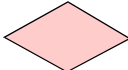
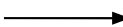
## Operator and function notation

- Two possible ways to express the same transformation of data
- *Examples:*

$a + b$	$sum(a,b)$
$(2 + 5) \times 4$	$product(sum(2,5), 4)$
$\sum_{k=1}^4 k$	$sum(1,2,3,4)$
- Here the name of a *function* could also be the name of a *module*, *subprogram*, or *Java method*

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## 4. Algorithm design tools

- Both notations show order of execution
  - Pseudocode
    - informal
    - precise
    - text outline format
  - Flowcharts
    - graphical
    - shapes denote steps
    - arrows show flow of control
- |   |               |
|---|---------------|
|  | Begin/end     |
|  | Processing    |
|  | I/O           |
|  | Decision test |
|  | Flow          |

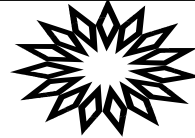
## Algorithm:

A precise plan to solve a problem in a finite number of steps



- Program designs use algorithms
- Most computation is algorithmic
- Flowcharts and pseudocode can express algorithms

# Algorithmic thinking

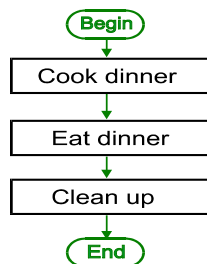


- *Definition:* an algorithm is a step-by-step plan to transform input to output in a finite number of steps
- Essential properties (L. Snyder):
  - Specification of input, output, relationship between them
  - Definiteness (deterministic sequence of operations)
  - Effectiveness (doability)
  - Finiteness

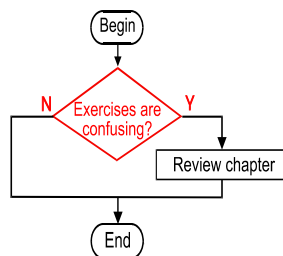
## Control structures

All algorithms may be built from three basic *control structures*:

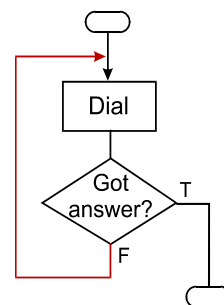
### Sequence



### Branch



### Loop



## The *sequence control structure*

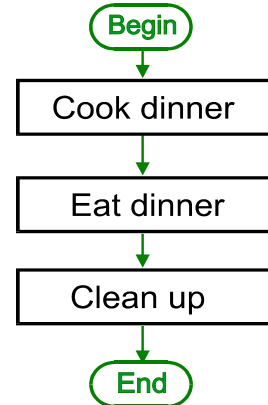
*Problem:*

Accomplish dinner routine

*Pseudocode:*

1. Cook dinner
2. Eat dinner
3. Clean up

*Flowchart:*



## An algorithm to add numbers

1. Prompt for integers  $input1$ ,  $input2$
2.  $sum \leftarrow input1 + input2$
3. Display  $sum$

- In pseudocode and flowcharts, the symbol  $\leftarrow$  stands for assignment of a value to a variable
- An algorithm is almost always *general purpose*: it works with *variables*, not only specific constant values

## The decision control structure

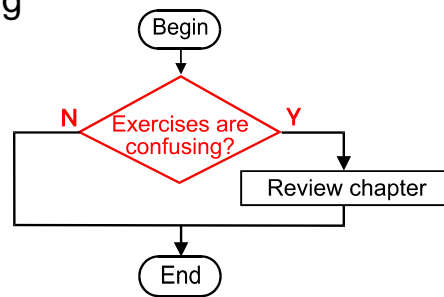
*Problem:*

Prepare to do homework

*Pseudocode:*

If exercises are confusing  
review chapter

*Flowchart:*



## Finding absolute value

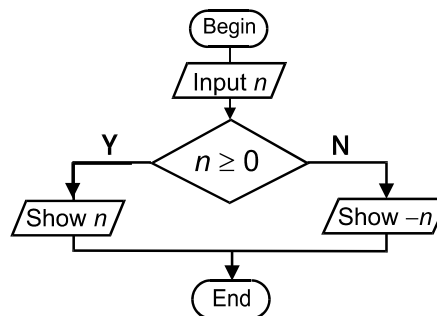
**Input  $n$**

**If  $n \geq 0$**

**display  $n$**

**otherwise**

**display  $(-n)$**

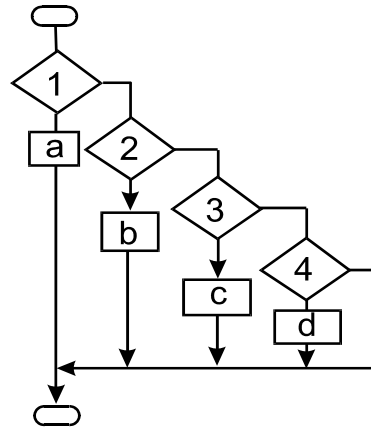


- With the branch control structure, one and only one of the alternatives executes
- In pseudocode, the subordinate (conditional) steps are normally indented

## Multiple alternatives

- Require multiple diamonds in flowchart

If  $n = 1$  display 'a'  
 otherwise  
 if  $n = 2$  display 'b'  
 otherwise  
 if  $n = 3$  display 'c'  
 otherwise  
 if  $n = 4$  display 'd'



## The *repetition* (loop) control structure

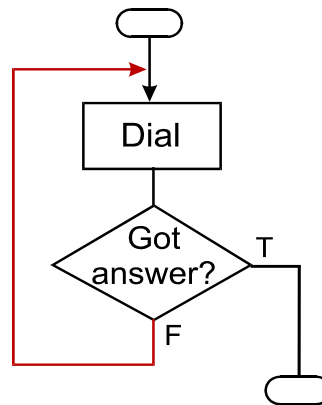
*Flowchart:*

*Problem:*

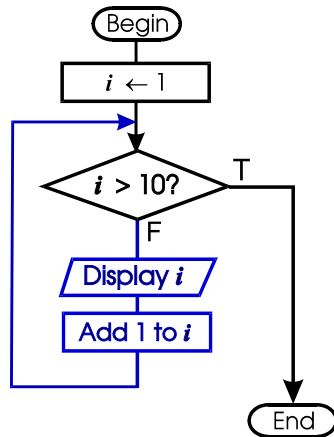
Telephone someone

*Pseudocode:*

Repeat  
 Dial number  
 until someone answers



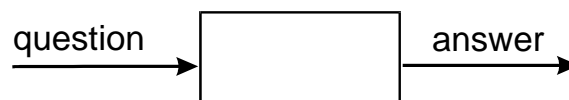
## Counting to 10



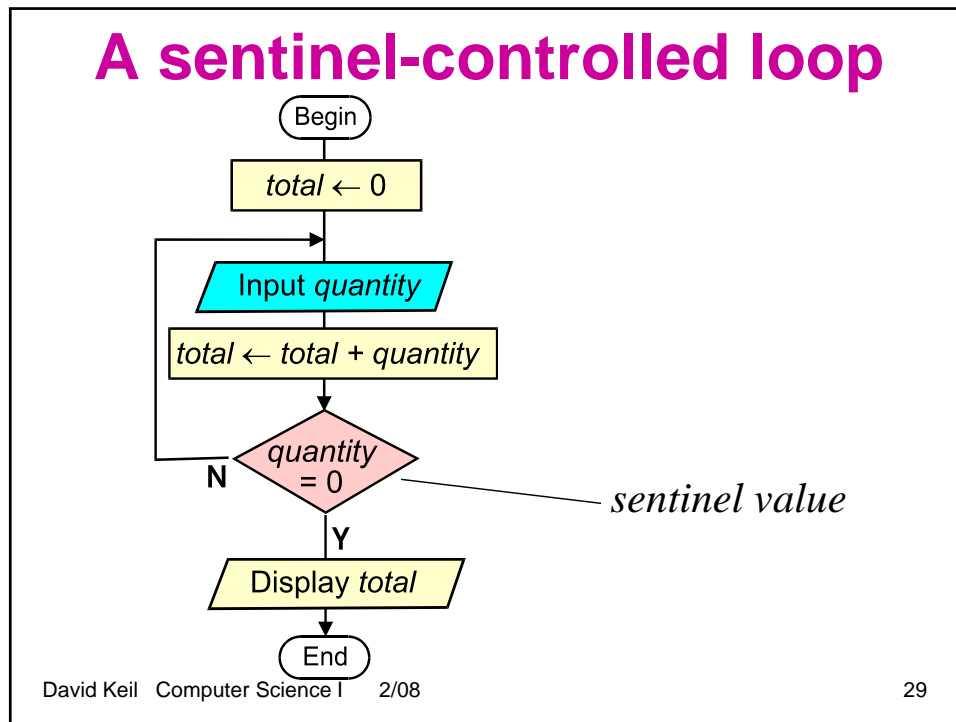
**Problem:** Display all values from 1 to 10

- A *counted* loop; counter is  $i$

## Ways to express an algorithm or process



- Natural language
- Design notation
  - Flowchart
  - Pseudocode
  - Unified Modeling Language (UML)
- Programming language (JavaScript, Java, C++...)



## Tracing an algorithm

- Allows designer to check result of algorithm, including internal (undisplayed) values
- Use one column per value traced; one row per loop iteration.
- *Example* (See previous slide):

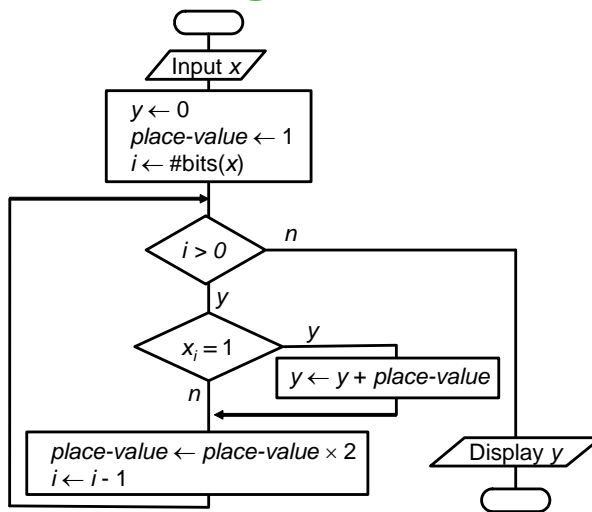
<i>quantity</i>	<i>total</i>	<i>output</i>
	0	
3	3	
2	5	
1	6	
0	6	6

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## Problem: binary to decimal

- *Problem:* Convert binary string to decimal value
- *Analysis:* Recall (Topic 4) that a numeral represents the *sum of place values*, which are each  $b^i$ , where  $b$  is base (2, 10, ...) and  $i$  is the number of places from the right
- *Solution* (see next slide):
  - Let  $x$  be input bit sequence,  $y$  be output value
  - Start at rightmost bit (counter  $i = \# \text{ bits}$ )
  - Loop through bits, R to L
  - At each 1-bit, add a power of 2 (place-value)
  - Double place-values, decrement  $i$  at each iteration of loop

## Binary-to-decimal algorithm



```

Input x
y ← 0
pv ← 1
i ← #bits(x)
While i > 0
    If xi = 1
        y ← y + pv
    pv ← pv × 2
    i ← i - 1
Display y
    
```

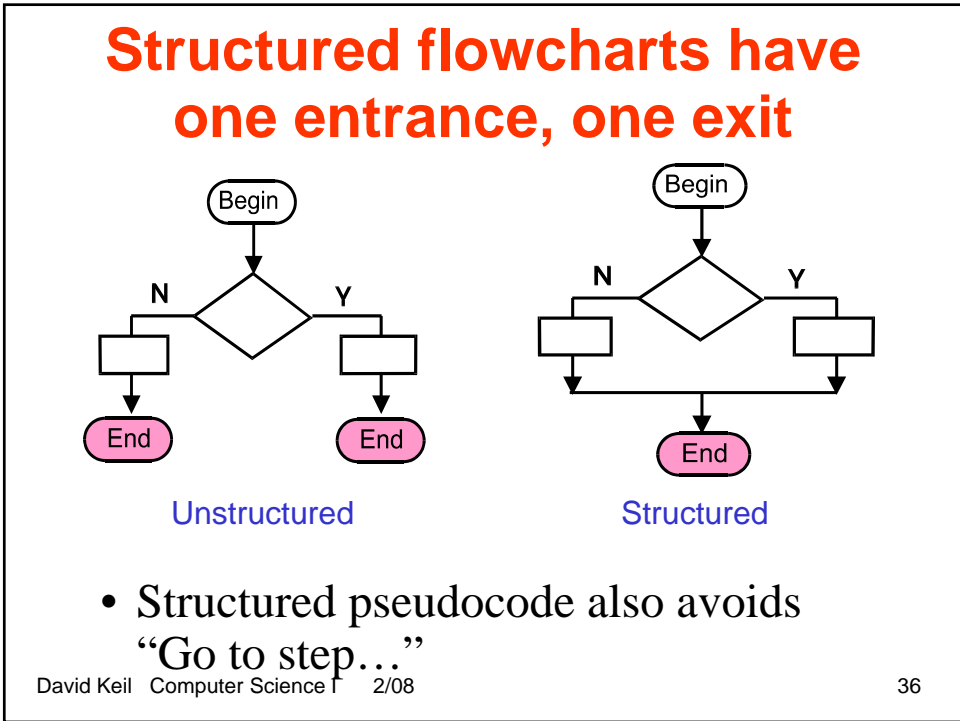
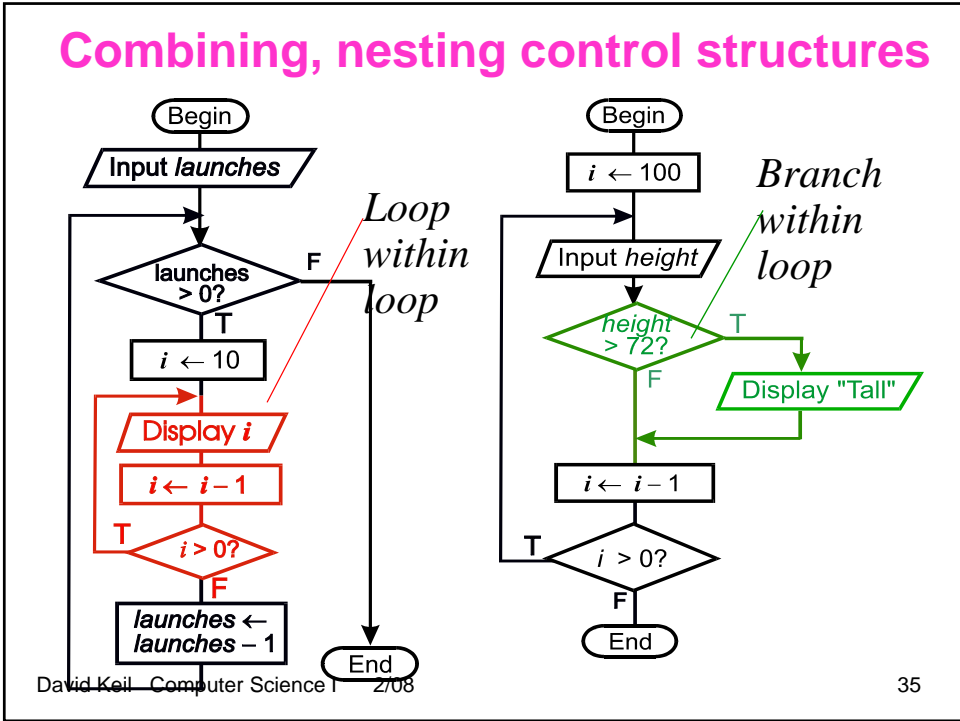
*Note*  $x_i$  is the  $i$ th bit of string  $x$ .  
*Example:* If  $x = '10'$  and  $i = 2$ , then  $x_i = '0'$

## Loop invariants

- A loop invariant is a logical (true/false) assertion about values and outputs at the beginning of a loop iteration
- *Example*  
Loop invariants for the previous slide are
  - The value of  $i$  is between 0 and 11
  - All values in  $\{1 \dots i - 1\}$  have been displayed
- Loop invariants help assure correctness

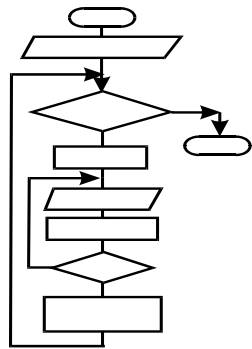
## Three control structures are sufficient

- Three control structures: *sequence*, *branch*, and *loop*
- They are used in structured programming; may be combined
- *Any computable problem* can be solve using only these three
- *Note:* Some problems are not computable

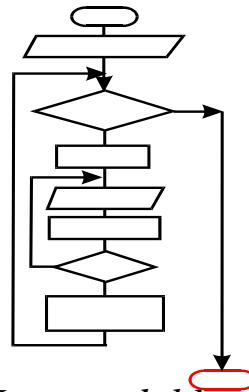


## The picture tells a story

- A flowchart should show what happens, at a glance



*Not too clear*



*More readable*

## 5. Functions and computation

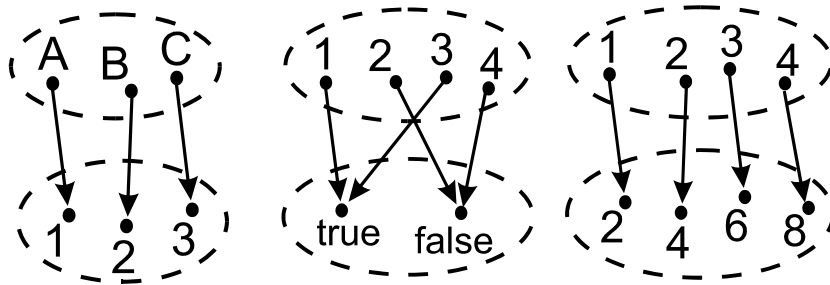
- A function in mathematics is a passive *set of pairs* that maps sets
- A computation entails *action*
- A computer program or subprogram computes a mathematical function
- A C or C++ “function” is actually a subprogram, not a mathematical function

## Review of functions

- *Function*: A set that is a mapping from one set to itself or to another set

- *Examples*:

$Index('B') = 2$        $Odd(3) = true$        $Twice(1) = 2$



## Computable functions

- A mapping obtained by an effective step-by-step procedure
- *Examples*: successor, sum
- Computer programming is concerned with coding computable functions
- An uncomputable function:  
“Does this program work correctly?”
- The computable functions are the same as the ones that are recursively definable

## Recursive functions and computable functions

- For natural numbers  $a, b$  in  $\{0, 1, 2, 3, \dots\}$ :

$$sum(a, b) = \begin{cases} b & \text{if } a = 0 \\ sum(a-1, b+1) & \text{otherwise} \end{cases}$$

- The definition of  $sum$  is *recursive* because it uses itself
- The form of this definition is a *recurrence*
- It guarantees computability

## Some recurrences

$$sum(a, b) = \begin{cases} b & \text{if } a = 0 \\ sum(a-1, b+1) & \text{otherwise} \end{cases}$$

$$product(a, b) = \begin{cases} 0 & \text{if } b = 0 \\ a & \text{if } b = 1 \\ a + product(a, b-1) & \text{otherwise} \end{cases}$$

$$even(a) = \begin{cases} true & \text{if } a = 0 \\ false & \text{if } a = 1 \\ even(a-2) & \text{otherwise} \end{cases}$$

## Russian peasants' algorithm

### Product (a, b)

```

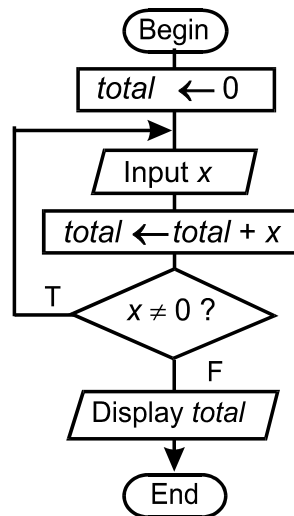
result ← 0
while a > 0
  if a is odd
    add b to result
  a ← ⌊a ÷ 2⌋
  b ← b × 2
Return result
    
```

Example:  $13 \times 5 = 65$

	<i>a</i>	<i>b</i>	<i>product</i>
			0
1.	13	5	5
2.	6	10	5
3.	3	20	25
4.	1	40	65
5.	0	80	

## Non-algorithmic computations

- The process diagrammed at right will never terminate if user continues to input a non-zero value
- Interaction, alternating input and output is not algorithmic,



## Generations of programming languages

- First generation: Machine languages (binary)
- 2<sup>nd</sup> generation: Assembler languages, processor specific
- 3<sup>rd</sup> generation: Procedural, high-level, hardware independent (C, BASIC, JavaScript)
- 4<sup>th</sup> generation: Nonprocedural query or report-generation languages (SQL, RPG)
- Declarative languages (Prolog)
- Object-oriented languages (Java)
- Functional languages (Lisp)

## References

- Cay Horstmann. *Big Java*, 3<sup>rd</sup> ed. Wiley, 2008.
- J. Parsons and D. Oja. *Computer Concepts*, 9<sup>th</sup> ed. Thomson, 2007.
- L. Snyder. *Fluency with Information Technology*. Addison Wesley, 2006.
- G. Schneider and J. Winters. *Applying Use Cases: A Practical Guide*. Addison Wesley, 1998.