# Increasing Communication and Problem-Solving Skills in a Liberal Arts Probability Course 

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## Overview

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- Why teach this way?
(2) Course Design
- Attendance/Participation
- Homework/Portfolio
- Individual Research Paper Project
(3) Conclusion


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- Oftentimes, students are exposed to advanced undergraduate mathematics courses (even in the liberal arts setting) in the form of watching a professor lecture at a blackboard.
- Students rarely speak in class, are not given opportunities to work with other students and the professor at the same time, and are passively engaged for long periods of time.


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- presenting solutions to homework problems in class on the blackboard and leading discussions, and
- working on individual research projects.
- This focus was done as my attempt to improve student engagement, develop stronger critical thinking skills, and improve collaboration and communication skills via written and oral work.

Why teach this way?

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- All students had taken Calculus I with minor knowledge of integration.
- Their only previous probability knowledge came from brief introductions in Elementary Statistics, Pre-Calculus, and advanced physics courses.


## Grading Weights

- Attendance/Participation - 10\%
- Homework/Portfolio - 60\%
- Individual Research Paper Project - 30\%


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- Fridays consisted of student presentations of two homework problems for that week and a discussion of the struggles and interesting findings of the week's content.


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- All homework assignments were corrected by me and revisions were suggested.


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- correct solutions to all homework problems assigned throughout the course, and
- a cover page, table of contents, and index referring to particular concepts and where they could be found in the portfolio.


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- At the end of the semester, students presented a project overview to the class that summarized the article and their paper.


## Papers Chosen

The particular papers chosen by the students were

- Chen, Shiu-Sheng. (2007) Does Monetary Policy Have Asymmetric Effects on Stock Returns? Journal of Money, Credit and Banking, Vol. 39, 667-688.
- Newell, G.F. (1959) A Theory of Platoon Formation in Tunnel Traffic. Operations Research, Vol. 7, No. 5, 589-598.
- Tversky, Amos, and Gilovich, Thomas. (2005) The Cold Facts About the "Hot Hand" in Basketball. Anthology of Statistics in Sports, 16:169.


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- Their initial annoyances with $\mathrm{AT}_{\mathrm{E}} \mathrm{X}$ turned into appreciation.
- It was very rewarding as the professor to see breakthroughs in understanding of concepts happen in class as I answered student questions and watched them interact with each other.


## Thank you for attending!

## Questions or comments?

